## US5256 LESSON TWO: ARITHMETIC AND GEOMETRIC SERIES

For each series: 1. calculate the next term,
2. write the expression for the $n$th term;
3. calculate $\mathrm{T}_{10}$
4. calculate the sum of the first 23 terms
a.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |  | $\boldsymbol{n}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{T}_{(n)}$ | 4 | 7 | 10 | 13 |  | $\mathrm{~T}_{(n)}=$ |  |  |

b.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\boldsymbol{n}$ | $\mathbf{1 0}$ | $\sum_{1}^{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~T}_{(n)}$ | 5.4 | 16.7 | 28 | 39.3 |  | $\mathrm{~T}_{(n)}=$ |  |  |

c.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{n}$ | $\mathbf{1 0}$ | $\sum_{1}^{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~T}_{(n)}$ | 12 | 6.5 | $\mathbf{1}$ | -4.5 |  | $\mathrm{~T}_{(n)}=$ |  |  |

d.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\boldsymbol{n}$ | $\mathbf{1 0}$ | $\sum_{1}^{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~T}_{(n)}$ | 7 | 13 | 19 | 25 |  | $\mathrm{~T}_{(n)}=$ |  |  |

2. What is the common difference for a series with $T_{8}=32$ and $T_{13}=67$ ?
3. Write the expression for a series with $\mathrm{T}_{1}=12.4$ and $\mathrm{T}_{5}=26$
4. Calculate the first four terms of a series with $\mathrm{T} 1=5$ and $\sum^{10}=59$
5. What is the first term of a series with $T_{18}=14$ and $T_{24}=-7$ ?
6. For the series with expression $T_{n}=3.5+(n-1) 5.4$, what is the sum of $T_{12}$ to $T_{19}$ ?

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a.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\boldsymbol{n}$ | $\mathbf{1 0}$ | $\sum_{1}^{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :--- | :--- | :--- |
| $\mathrm{~T}_{(n)}$ | 4 | 8 | 16 | 32 |  | $\mathrm{~T}_{(n)}=$ |  |  |

b.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\boldsymbol{n}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{T}_{(n)}$ | 5.4 | -5.4 | 5.4 | -5.4 |  | $\mathrm{~T}_{(n)}=$ |  |  |

c.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{n}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{T}_{(n)}$ | 12 | 36 | 108 | 324 |  | $\mathrm{~T}_{(n)}=$ |  |  |

d.

| $\boldsymbol{n}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\boldsymbol{n}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{T}_{(n)}$ | 4 | -10 | 25 | -63 |  | $\mathrm{~T}_{(n)}=$ |  |  |

2. What is the common ratio for a series with $T_{3}=32$ and $T_{6}=512$ ?
3. Write the expression for a series with $\mathrm{T}_{1}=12.4$ and $\mathrm{T}_{5}=21420.75$
4. Calculate the sum of the first 40 terms of:
a. $3+6-12+24-\ldots$
b. $15+45+135+405+\ldots$
c. $\frac{2}{5}+\frac{6}{10}+\frac{18}{20}+\frac{54}{40}+$
5. Write the first four term of a series with $T_{1}=14$ and $S_{\infty}=18.67$
6. Each day, Jack's beanstalk has gained $2 / 3$ of the previous day's growth. If it grew 20 metres in its first day after germination, how tall was it after two weeks?
